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RECURSION OPERATORS AND REDUCTIONS OF INTEGRABLE EQUATIONS ON SYMMETRIC SPACES*

VLADIMIR S. GERDJIKOV, ALEXANDER V. MIKHAILOV † and TIHOMIR I. VALCHEV

Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, 1784 Sofia, Bulgaria

†Applied Mathematics Department, University of Leeds, Leeds, LS2 9JT, UK

Abstract. We study certain classes of integrable nonlinear differential equations related to the type symmetric spaces. Our main examples concern equations related to **A.III**-type symmetric spaces. We use the Cartan involution corresponding to this symmetric space as an element of the reduction group and restrict generic Lax operators to this symmetric space. Next we outline the spectral theory of the reduced Lax operator L and construct its fundamental analytic solutions. Analyzing the Wronskian relations we introduce the 'squared solutions' of L and derive the recursion operators by three different methods.

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