

GEOMETRICAL INTERPRETATION OF TIME-DEPENDENT SPIN PHASES

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ABSTRACT

The Pancharatnam and Aharonov-Anandan phases for spin in a rotating magnetic field are interpreted and represented geometrically using spherical triangle.

1. Introduction

Berry's article "Quantal phase factors accompanying adiabatic changes"¹ induced a renewal of interest in phases and phase differences in quantum mechanics.²⁻⁵ As distinct from the standard quantum mechanics^{6,7} which makes emphasis on the measurability of absolute squares of wave functions, in the works which follow Berry's paper the emphasis is on the measurability of phases (phase differences).^{8,9}

A careful analysis shows that the conditions of measurability of phases (phase differences) in Berry's and subsequent works are: 1) the existence of interference of two states φ_1 and φ_2 which belong to the same ray - $\varphi_2 = \varphi_1 e^{i\beta}$; 2) the possibility to measure the intensity of their superposition $I = |\varphi_1 + \varphi_2|^2 = 2|\varphi_1|^2(1 + \cos\beta)$.

But, standard quantum mechanics is insisting on the following statement: If, in a Hilbert space \mathcal{H} , $|\varphi\rangle$ represents a physical state of the system, all vectors of the form $e^{i\beta}|\varphi\rangle$, β real, represent the same physical state and are said to form a ray. Also, standard quantum mechanics does not interpret intensity measurements in interference experiments as phase measurements. Instead, in standard quantum mechanics one usually argues that relative phases play an important role.⁶

Berry,¹ Kwiat and Chiao,⁹ Jiao et al.⁸ avoided to comment explicitly this departure from standard quantum mechanical thinking. Instead, different attributes were given to particular phases which were studied,² like: geometrical, adiabatic, topological, non-integrable, mysterious etc. It seems to us that in this way has